

# Geometry

## 1<sup>st</sup> prep. – 2<sup>nd</sup> term

- ❖ If two straight lines intersect then the measures of each two vertically opposite angles are equal
- ❖ The sum of the measures of the accumulative angles at a point is equal to  $360^\circ$
- ❖ The simple line is the line that does not cut itself
- ❖ The non simple line is the line that cuts itself once or more
- ❖ The polygon is a simple closed line that consists of three line segments or more
- ❖ The polygon is named according to the number of its sides
- ❖ Triangle ( 3 sides )      Quadrilateral ( 4 sides )      Pentagon ( 5 sides )  
 Hexagon ( 6 sides )      Heptagon ( 7 sides )      Octagon ( 8 sides )  
 Nonagon ( 9 sides )      Decagon ( 10 sides )
- ❖ Convex polygon has any interior angle less than  $180^\circ$
- ❖ Concave polygon has one or more angle more than  $180^\circ$
- ❖ The number of triangles of any polygon is  $(n - 2)$        $n$  – number of sides
- ❖ The sum of measures of the interior angles of a polygon is  $(n - 2) \times 180$
- ❖ The sum of measures of the exterior angles of a convex polygon of  $n$  sides =  $360^\circ$
- ❖ The regular polygon has all sides and angles are equal
- ❖ The measure of each interior angle of the regular polygon is  $\frac{(n - 2) \times 180}{n}$
- ❖ The number of diagonals of the polygon is  $\frac{n(n - 3)}{2}$
- ❖ In the quadrilateral ABCD if  $m \angle(A) = 2m \angle(B) = m \angle(C) = 96^\circ$   
 Then  $m \angle(D) = 120^\circ$
- ❖ A parallelogram is a quadrilateral in which each two opposite sides are parallel
- ❖ The properties of a parallelogram:
  - 1-The sum of measures of each two consecutive angles in a parallelogram is  $180^\circ$
  - 2- In a parallelogram each two opposite angles are equal in measure
  - 3- In a parallelogram each two opposite sides are equal in length
  - 4- The two diagonals in a parallelogram bisect each other

- ❖ A rectangle is a parallelogram with a right angle and the diagonals are equal in length
- ❖ A rhombus is a parallelogram in which two adjacent sides are equal in length and the two diagonals are perpendicular
- ❖ A square is a parallelogram with a right angle and two adjacent sides equal in length and two diagonals perpendicular and equal in length

❖ **Theorem (1)**

The sum of the measures of the interior angles of a triangle is  $180^\circ$

- ❖ The measure of the exterior angle of a triangle is equal to the sum of the measures of its Non adjacent interior angles

- ❖ In  $\triangle ABC$  if

$$m\angle A + m\angle B = m\angle C$$

then  $m\angle C = 90^\circ$  (right angle)

$$m\angle A + m\angle B > m\angle C$$

then  $m\angle C$  is acute angle

$$m\angle A + m\angle B < m\angle C$$

then  $m\angle C$  is obtuse angle

❖ **Theorem (2)**

The ray drawn from the midpoint of a side of a triangle parallel to another side bisect the third side

❖ **Corollary**

The line segment joining the midpoints of two sides of a triangle is parallel to the Third side

❖ **Theorem (3)**

The length of the line segment joining the midpoints of two sides of a triangle is Equal to half the length of the third side

- ❖ The image of the point  $(X, Y)$  by reflection in the X – axis is  $(X, -Y)$
- ❖ The image of the point  $(X, Y)$  by reflection in the Y – axis is  $(-X, Y)$
- ❖ The image of the point  $(X, Y)$  by reflection in the origin point is  $(-X, -Y)$
- ❖ The image of the point  $(X, Y)$  by translation  $(K, L)$  is  $(X + K, Y + L)$

*with my Best wishes*  
*Mr. Mahmoud taha*

MAhmmoud